

Provably Secure ID-Based Signature without Trusted PKG for Smart Grid

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Abstract—By using Gap Diffie-Hellman groups, we construct an efficient ID-based signature scheme without trusted PKG for smart grid, which security relies on the hardness of the Computational Diffie-Hellman Problem (CDHP). In this scheme, PKG is prevented from forging a legal user's signature because it only generates the partially private key. The scheme is proved to be secure against existential forgery on adaptively chosen message and ID attack, assuming CDHP is intractable. Our scheme not only satisfies security properties but also has a higher efficiency.

Keywords—smart grid; key escrow; id-based signature; random oracle model

I. INTRODUCTION

In traditional CA-based Cryptosystems, the binding between public key and identity of the signer is obtained via a digital certificate, issued by a Trusted Third Party called Certifying Authority (CA). To simplify the certificate management process, an ID-based Cryptosystem (IBC) based on integer factorization problem was proposed by Shamir [1], which allows a user to use his identity as the public key. But there are some drawbacks in ID-based systems. The most criticism against ID-based systems is that PKG knows the private key of all users, so it is able to impersonate any user to sign a document or decrypt an encrypted message. It implies that the PKG must be trusted unconditionally otherwise the systems will soon be collapsed. However, it would be difficult to assume the existence of a trusted party in smart grid, where the communication parties are changing frequently.

Several ID-based signature schemes based on the bilinear maps (pairings) have been proposed. These include Cha and Cheon's [2] scheme and Hess' [3] scheme. They gave a formal definition of unforgeability of ID-based signature against chosen message attack and proved that their schemes are secure in the random oracle model assuming the Computational Diffie-Hellman (CDH) problem is computationally intractable. Al-Riyami and Paterson [4] introduced and developed the notion of certificateless public key cryptography (CL-PKC). CL-PKC is a model for the use of public key cryptography, which is intermediate between the identity-based and traditional PKI approaches. In [5],

the authors proposed an ID-based signature without trusted PKG from bilinear pairings. Gorantla and Saxena [6] proposed an efficient certificateless signature scheme. But their scheme was shown to be insecure [7]. Liu et al. [8] proposed an ID-based signature without trusted Private Key Generator, which solved the key escrow problem by binding two public key with a same identity.

In this paper, we assume that there is only one PKG in our systems and the PKG is not a trusted party anymore. In our systems, if the dishonest PKG impersonate an honest user to sign a document, the user can provide a proof that the PKG is dishonest.

The rest of the paper is organized as follows. The formal model of a secure ID-based signature without trusted PKG is presented in Section II. In Section III, the proposed ID-based signature scheme is presented. The security and efficiency analysis of our schemes are given in Section IV. Finally, Section V concludes this paper.

II. BASIC MODELS

A. Framework of ID-based Signature without trusted PKG

An ID-based signature scheme without trusted PKG consists of four algorithms: **Setup**, **Extract**, **Sign** and **Verify**.

Setup: This algorithm is usually executed by the private key generator (PKG). On a unary string input 1^k where k is a security parameter, it produces the public parameters $params$, which includes a description of a finite signature space, a description of a finite message space. The master secret x_{PKG} is also the output, which is kept secret.

Extract: On an arbitrary string input id , it computes the private signing key (x_1, x_2) with the help of master secret x_{PKG} , and the corresponding public verification key (y_1, y_2) .

Sign: Suppose the requester wants a message m to be signed, after the execution of Sign algorithm, a signature σ will be produced.

Verify: Input a signature σ , a message m and the signer's public verification key (y_1, y_2) , it outputs "true"

or “false”, depending on whether σ is a valid signature signed by the signer.

B. Attack Model for ID-based Signature without trusted PKG

We define unforgeability through the following game between a challenger C and an attacker A .

Setup: The challenger C takes a security parameter k and runs the Setup algorithm. C sends the public system parameters to the attacker A and keeps the master key x_{PKG} itself.

Attack: The attacker A adaptively performs the following three queries:

(1) *Hash functions queries:* C returns a hash value for the requested input.

(2) *Extract queries:* When A submits an identity id , C runs Extract algorithm to return the private key x_2 .

(3) *Sign queries:* When A submits (id, m) (id is a chosen identity by A) to ask a signature, C runs Sign algorithm with the attacker A . Then A obtains a valid signature $\sigma = \text{Sign}(id, m, x_1, x_2)$.

Forgery: The attacker A outputs a forged signature (σ, m) , where m is a plaintext message. A wins the game if σ is a valid signature of m for id in the following three cases.

The adversary A maybe forge a signature colluding with a dishonest PKG. Thus there are three cases [9] to discuss.

Case 1: PKG is honest. A forges a valid signature with no help of a trusted PKG.

Case 2: PKG is semi-honest. In this case A has a piece of additional information x_2 from the PKG.

Case 3: PKG is malicious. It wants to impersonate an honest user whose identity information is id , A forges a valid signature of the honest user.

Using this attack model, we can reduce the security of ID-based signature without trusted PKG to the hardness of CDHP.

Definition 1. An ID-based signature scheme is said to be existential unforgeable against adaptive chosen-message-and-identity attacks if no adversary has a non-negligible advantage in the above game.

III. ID-BASED SIGNATURE SCHEME WITHOUT TRUSTED PKG

Let G_1 be a cyclic additive group generated by P with the prime order q . We introduce the following mathematical problems in G_1 .

(1) Discrete Logarithm Problem (DLP): Given two elements $P, Q \in G_1$, to find an integer $n \in Z_q^*$, such that $Q = nP$ whenever such an integer exists.

(2) Decision Diffie-Hellman Problem (DDHP): Given $P, aP, bP, cP \in G_1$ for $a, b, c \in Z_q^*$, to decide whether $c \equiv ab \pmod{q}$.

(3) Computational Diffie-Hellman Problem (CDHP): Given $P, aP, bP \in G_1$ for $a, b \in Z_q^*$, to compute abP .

We assume through this paper that CDHP and DLP are intractable. When the DDHP is easy but the CDHP is hard on the group G_1 , we call G_1 a Gap Diffie-Hellman (GDH) group.

In this section, we first define two cryptographic hash functions $H_1: \{0,1\}^* \rightarrow G_1, H_2: \{0,1\}^* \times G_1 \rightarrow Z_q^*$.

Setup: PKG randomly chooses $s_{PKG} \in Z_q^*$ and sets $Q_{PKG} = s_{PKG}P$. The public parameters of the system are $params = \{G_1, G_2, e, P, q, Q_{PKG}, H_1, H_2\}$. PKG keeps s_{PKG} secretly as the master key.

Extract: A user submits his identity information id and authenticates himself to PKG. The user then randomly chooses an integer $s_1 \in Z_q^*$ as his partially secret key and computes $Q_1 = s_1P$ as his partially public key. Suppose the signer's identity is given by the string id , the other partially secret key of the identity is then given by $S_2 = s_{PKG}Q_2$ where $Q_2 = H_1(id, Q_1)$, which is computed by the PKG and given to the signer. For a signer, (Q_1, Q_2) is his public key and (s_1, S_2) is his private key.

Sign: To sign a message m , the signer chooses a random integer $k \in Z_q^*$:

(1) $U = kP, r = H_2(m, U)$;

(2) $V = rs_1Q_2 + rS_2 = r(s_1Q_2 + S_2)$;

The signature is then the pair (U, V) .

Verify: On receiving a message m and signature (U, V) the verifier computes:

(1) $Q_2 = H_1(id, Q_1), r = H_2(m, U), T = Q_1 + Q_{PKG}$;

(2) Accept the signature if and only if $e(V, P) = e(Q_2, T)^r$.

It is straightforward to check that the verification equation holds for a valid signature.

IV. SECURITY AND EFFICIENCY ANALYSIS OF OUR SCHEME

A. Security

Theorem 1 (Correctness) Our scheme in section III is correct.

Proof:

$$\begin{aligned} & e(V, P) \\ &= e(rs_1Q_2 + rS_2, P) \\ &= e(r(s_1Q_2 + s_{PKG}Q_2), P) \\ &= e(rQ_2, (s_1 + s_{PKG})P) \\ &= e(rQ_2, Q_1 + Q_{PKG}) \\ &= e(Q_2, T)^r \end{aligned}$$

This theorem is proved.

Theorem 2 Our ID-based signature scheme is secure against on existential adaptively chosen message and ID attacks under the assumption of CDHP is hard in G_1 and random oracle model.

Proof: We referred to the proof of unforgeability of the signature scheme by Pointcheval and Stern [10,11]. There are three cases to discuss:

Case 1: PKG is honest. A forges a valid signature with no help of a trusted PKG.

We suppose that H_1, H_2 are random oracles, and there exists a probabilistic polynomial time Turing machine A whose input only consists of public data. We assume that A can make q_1 queries to the random oracle H_1 , q_2 queries to the random oracle H_2 and q_s queries to the signing oracle.

C gives A the system parameters $Q_{PKG}=aP$, Note that a is unknown to C . This value simulates the master key value for the PKG in the game.

H_1 -Queries: A can query the random oracle H_1 at any time. C simulates the random oracle by keeping list of couples $(\Sigma_i, Q_{(2,i)})$ which is called the L_1 -List, where Σ_i is a couple of $(id_i, Q_{(1,i)})$. When the oracle is queried with an input Σ , C responds as follows:

1. If the query Σ is already on the L_1 -List in the couple $(\Sigma, Q_{(2,i)})$, then C outputs $Q_{(2,i)}$.
2. Otherwise C selects a random Q_2 , outputs Q_2 and adds (Σ, Q_2) to the L_1 -List.

Extract-Queries: A can query the partially private key for any identity id_i and the public key.

If $Q_{(2,i)} \neq H_1(id_i, Q_{(1,i)})$, C returns invalid. Otherwise, it outputs the partially private key $S_{(2,i)}$ corresponding to id_i which is obtained by running *Extract* algorithm.

H_2 -Querier: A can query the random oracle H_2 at any time. C simulates the random oracle by keeping list of couples (Σ_i, r_i) which is called the L_2 -List, where Σ_i is a triple of (m_i, U_i) . When the oracle is queried with an input Σ , C responds as follows:

1. If the query Σ is already on the L_2 -List, then C outputs the same answer.
2. Otherwise C selects a random r_i , outputs r_i and adds (Σ, r_i) to the L_2 -List.

Sign-Queries: For a sign request on m , C simulates the value of H_2 in the way as mentioned above. (U', V') will be used as the answer, where

$$\text{Verify}(id, m, Q_1, Q_2, U', V') = \text{True}.$$

It follows from the forking lemma [11] that if A is a sufficiently efficient forger in the above interaction, then we can construct a Las Vegas machine A' that outputs two signed messages $((id_i, m), U_1, V_1)$ and $((id_i, m), U_2, V_2)$ with $r_1 \neq r_2$. So we have the following equations.

$$\begin{aligned} V_1 &= r_1 s_1 Q_2 + r_1 S_2 \\ V_2 &= r_2 s_1 Q_2 + r_2 S_2 \end{aligned}$$

From above equations we can get the following equation.

$$(r_1 - r_2)^{-1}(V_1 - V_2) = (s_1 + s_{PKG})Q_2$$

Let $Q_2 = bP$ then $(s_1 + s_{PKG})P, bP \rightarrow (s_1 + s_{PKG})bP$. If A succeeds in time $\leq T$ with probability $\epsilon \geq 10(q_s + 1)(q_s + q_2)/2^k$, then C can solve the CDH problem in expected time $\leq 120686q_2 2^n T / 10(q_s + 1)(q_s + q_2)$ [11].

Case 2: PKG is semi-honest. In this case A has a piece of additional information S_2 from the dishonest PKG. C gives A the parameters $Q_{PKG} = aP$, Note that a is unknown to C . This value simulates the master key value for the PKG in the game.

The same as case 1, C can play the simulation twice so that A should produce two valid signature $((id_i, m), U_1, V_1)$ and $((id_i, m), U_2, V_2)$ with $r_1 \neq r_2$. Now we could get the following equations.

$$\begin{aligned} V_1 &= r_1 s_1 Q_2 + r_1 S_2 \\ V_2 &= r_2 s_1 Q_2 + r_2 S_2 \end{aligned}$$

From above equations we can get the following equation.

$$(r_1 - r_2)^{-1}(V_1 - V_2) = (s_1 + s_{PKG})Q_2$$

Let $Q_2 = bP$ then $(s_1 + s_{PKG})P, bP \rightarrow (s_1 + s_{PKG})bP$. If A succeeds in time $\leq T$ with probability $\epsilon \geq 10(q_s + 1)(q_s + q_2)/2^k$, then C can solve the CDH problem in expected time $\leq 120686q_2 2^n T / 10(q_s + 1)(q_s + q_2)$.

Case 3: PKG is malicious. It wants to impersonate an honest user whose identity information is id , A forges a valid signature of the honest user.

Suppose PKG wants to impersonate an honest user whose identity information is id . It can do as follows:

- 1, PKG randomly chooses $s'_i \in Z_q^*$ and computes

$$Q'_i = s'_i P, Q'_i = H_1(id, Q'_i), S'_i = s_{PKG} Q'_i.$$

- 2, It then performs the above signing protocol for the message m and output (U', V') .

PKG successfully forged a “valid” signature of the target user for the message m . However, the user can provide a proof to convince that the signature is forged by PKG. It first sends Q_1 to the arbiter, and then provides a “knowledge proof” that it knows $S_2 = s_{PKG} Q_2$, where $Q_2 = H_1(id, Q_1)$. The arbiter randomly chooses a secret integer $a \in Z_q^*$ and sends aP to the user; the user then computes $e(S_2, aP)$.

If the equation $e(S_2, aP) = e(Q_2, Q_{PKG})^a$, the arbiter deduces that PKG is dishonest because the master-key s_{PKG} is only known to him.

B. Efficiency

Here, we compare our ID-based signature scheme with the existing schemes in terms of computational power and show the summary in Table 1. In the table 1, Pa denotes the number of pairing operation, G_1A denotes the number of addition in G_1 , G_1M denotes the number of multiplication in G_1 , G_2E denotes the number of exponentiation in G_2 , G_2M denotes the number of multiplication in G_2 .

The new scheme has much pre-computation, so it has higher efficiency than the existing schemes. From Table 1, it is easy to see that our ID-based signature scheme is more efficient.

TABLE I COMPARISON OF COMPUTATION COST WITH EXISTING SCHEME

Algorithm	Pre-Sign	Sign
AP[4]	$1Pa$	$2G_1M+1G_1A+1G_2E$
CZK[5]	/	$3G_1M+1G_1A$
GS[6]	/	$2G_1M+1G_1A$
LSKW[8]	$1Pa+1G_1M$	$2G_1M+1G_1A+1G_2E$
Our Scheme	$1G_1M+1G_1A$	$2G_1M$

Algorithm	Pre-Verify	Verify
AP[4]	/	$4Pa+1G_2M+1G_2E$
CZK[5]	/	$4Pa+1G_1M$
GS[6]	/	$3Pa+1G_1M+1G_2M$
LSKW[8]	$1Pa$	$1Pa+1G_2M+1G_2E$
Our Scheme	$1Pa+1G_1A$	$1Pa+1G_2E$

V. CONCLUSION

In this paper, we have proposed a new ID-based signature scheme without trusted PKG for smart grid. Our scheme is proved to be secure against existential forgery on adaptively chosen message and ID attack, assuming CDHP is intractable. In our systems, if the

dishonest PKG impersonation an honest user to sign a document, the user can provide a proof that the PKG is dishonest. The scheme not only satisfies security properties but also has a higher efficiency.

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